W1 - Lesson 5: Number Operations with Decimals
Important Concepts of Grade 6 Mathematics

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Materials Required: A textbook is not needed. This is a stand-alone course.

Mathematics Grade 6
Version 5
Preview/Review W1 - Lesson 5

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W1 - Lesson 5:
Number Operations with Decimals
OBJECTIVES

By the end of this lesson, you should

- understand the purpose of the decimal point in a number
- add and subtract numbers that have decimal points
- multiply and divide numbers that have decimal points

GLOSSARY

decimal point - separates the whole numbers from the numbers that are less than one

difference - the answer in subtraction

factors - numbers used to form a product

product - the answer in multiplication

quotient - the answer in division

sum - the answer in addition
W1 - Lesson 5: Number Operations with Decimals

Welcome to W1 - Lesson 5! In this lesson you will be doing basic calculations (addition, subtraction, multiplication and division) with decimals. After practicing your skills in the four basic operations, you will be applying your knowledge of decimals in problem solving situations. Most errors committed when working with decimals are in the actual placing of the decimal point. **Remember:** Check your work to ensure that you are placing the decimal point in the correct position.

Addition and Subtraction With Decimals

The **decimal point** separates the whole numbers from the numbers that are less than one. The decimal point is located between the ones place value location and the tenths place value location.

When writing numbers in columns to do addition and subtraction, be sure that the **decimals are lined up in a straight vertical line**. Line up the decimals and place the decimal point in your answer before you begin calculations. You may also want to insert zeroes in empty place value locations.

**Examples:**

\[
\begin{array}{c}
24.73 \\
+ 674.9 \\
\hline
\end{array}
\quad \begin{array}{c}
24.73 \\
+ 674.90 \\
\hline
\end{array}
\]

Line up the decimals and put the decimal points in the answers.

Insert place holder zeroes. In subtraction, this is necessary.

\[
\begin{array}{c}
761.4 \\
- 348.66 \\
\hline
\end{array}
\quad \begin{array}{c}
761.40 \\
- 348.66 \\
\hline
\end{array}
\]

**Sum** - the answer in addition.

**Difference** - the answer in subtraction.
Questions

1. Calculate the answers. Place the decimal point in the answer before you begin calculations:

\[
\begin{array}{ccc}
345.6 & + & 129.862 \\
56.78 & + & \phantom{+} \\
623.01 & + & \phantom{+} \\
\hline
445.98 & + & 565.765 \\
\end{array}
\]

\[
\begin{array}{ccc}
78.84 & + & 0.368 \\
-19.06 & - & 0.2947 \\
\hline
59.78 & - & 0.6627 \\
\end{array}
\]

2. In the space provided below, write the following addition questions in vertical columns and find the sums. Remember to keep the decimal points in vertical straight lines. Place the decimal point in the answer before you begin calculations.

a. \[23.45 + 123.8 + 98.65 + 34.665 =\]

b. \[98.076 + 6.657 + 543.5 + 102.345 =\]
c. \[ 0.639 + 654.2 + 34.561 + 79.949 = \]

d. \[ 456.12 + 5.3 + 99.66 + 37.835 = \]

3. In the space provided below, write the following subtraction questions in vertical columns and find the differences. Remember to keep the decimal points in vertical straight lines. In subtraction, inserting place-holder zeroes is very important. Place the decimal point in the answer before you begin calculations.

a. \[ 387.56 - 287.62 = \]  
b. \[ 6708.3 - 836.67 = \]

c. \[ 56.789 - 49.78 = \]  
d. \[ 882.34 - 97.184 = \]

e. \[ 123.903 - 98.98 = \]
4. Charlie has a summer job working with a landscaping company. He made a list of items he wants to buy when he gets paid: blue jeans $69.90, wristwatch $83.50, running shoes $109.95, CDs $24.95 each, shorts $14.99 and T-shirts $21.69. Use the space below to do your calculations.

a. Charlie purchased the following items: 2 T-shirts, 2 pair of shorts, 4 CDs and one of each of the other items. Calculate how much money he spent.

b. Charlie paid the clerk six $50.00 bills and seven $20.00 bills. How much change did he get back?
5. Use the following table to answer the questions below.

<table>
<thead>
<tr>
<th>Name</th>
<th>Height (cm)</th>
<th>Weight (kg)</th>
<th>Age (Days)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Anthony</td>
<td>151.91</td>
<td>45.0</td>
<td>4015</td>
</tr>
<tr>
<td>Elizabeth</td>
<td>139.83</td>
<td>36.781</td>
<td>4137</td>
</tr>
<tr>
<td>Jackie</td>
<td>157.26</td>
<td>54.63</td>
<td>4311</td>
</tr>
<tr>
<td>Wilbur</td>
<td>161.42</td>
<td>39.07</td>
<td>4218</td>
</tr>
</tbody>
</table>

a. Calculate the total weight of the 4 students.

b. Calculate the total height of the 4 students.

c. Calculate how much taller Wilbur is than Elizabeth.

d. How many days older than Elizabeth is Wilbur?

e. Calculate how much lighter Anthony is than Jackie.
Multiplying with Decimals

Terms used in Multiplication -

- 24 ← multiplicand
- ×35 ← multiplier
- 120
- 720
- 840 ← product

The multiplicand and multiplier are also known as factors.

Product - the answer in multiplication.

Multiplying with decimals is the same as multiplying without decimals; you just need to place the decimal point in the correct location. Once you have completed the multiplication, you must carefully decide where to place the decimal point. Count the number of digits to the right of the decimal point (called decimal places) in the multiplicand and the multiplier. Then, give the product the same number of decimal places.

\[
\begin{align*}
25 & \quad \leftarrow 0 \text{ decimal places} \\
\times 2.4 & \quad \leftarrow 1 \text{ decimal place} \\
100 & \\
500 & \\
60.0 & \quad \leftarrow 1 \text{ decimal place in the answer}
\end{align*}
\]

A total of one decimal place is in the multiplicand and multiplier. Therefore, we must have one decimal place in the product.

\[
\begin{align*}
0.32 & \quad \leftarrow 2 \text{ decimal places} \\
\times 4.1 & \quad \leftarrow 1 \text{ decimal place} \\
32 & \\
1.280 & \\
1.312 & \quad \leftarrow 3 \text{ decimal places}
\end{align*}
\]

A total of 3 decimal places is in the multiplicand and multiplier. Therefore, we must have 3 decimal places in the product.
Questions

1. In the space provided below, write the questions in vertical columns and calculate the answers. Remember to count the number of decimal places in the multiplicand and multiplier to have the total number in the product.

   a. \( 3.5 \times 42 = \)
   
   b. \( 6.7 \times 3.9 = \)

   c. \( 0.69 \times 0.85 = \)
   
   d. \( 0.78 \times 8.2 = \)

   e. \( 295 \times 0.145 = \)
2. The 10th place finisher in a pro golf tournament wins $17,281.50. The 2nd place winner makes 8 times this amount. How much money does the 2nd place winner receive?

3. A certain racing bicycle wheel travels 2.68 metres in one rotation. In one race, the rider averaged 36 rotations every minute. At this speed, how far did the bicycle travel in 15 minutes?

4. Crystal has $27.85 and Suhal has $34.65. Amber has 8.5 times more money than Crystal and Suhal combined. How much money does Amber have?
Dividing with Decimals

Terms Used in Division

\[
\begin{array}{c|c|c}
\text{divisor} & 6 & \text{quotient} \\
\hline
\text{dividend} & 56.76 & \text{dividend} \\
\hline
54xx & 27 & 24 \\
\hline
36 & 36 & 0 \\
\hline
\end{array}
\]

Before you begin dividing, place the decimal point in the quotient. It should be in the same place value location as the decimal in the dividend.

\[
18 \overline{) 8.82} \quad 6 \overline{) 56.76}
\]

The easiest way to deal with a one-decimal-place divisor is to change it to a whole number by multiplying it by 10. Multiply both the divisor and the dividend. If the divisor has two-decimal-places, multiply by 100.

A division question with a one-decimal-place divisor:

\[
0.6 \overline{) 4.8} \quad 6 \overline{) 48}.
\]

(before we multiply by 10) \quad (after we multiply by 10)

When we multiply 0.6 × 10, the answer is 6. When we multiply 4.8 × 10, the answer is 48.

A division question with a two-decimal-place divisor:

\[
0.25 \overline{) 17.75} \quad 25 \overline{) 1775}.
\]

(before we multiply by 100) \quad (after we multiply by 100)

When we multiply 0.25 × 100, the answer is 25. When we multiply 17.75 × 100 the answer is 1775.

Quotient - the answer in division.
Questions

1. In the space provided below answer the following questions by calculating the answers. If the divisor has one-decimal-place, multiply both the divisor and dividend by 10. If the divisor has two-decimal-places, multiply both the divisor and dividend by 100. Check that the decimal is in the correct position in the quotient.

   a. $5.76 \div 8 =$  
   b. $10.20 \div 12 =$  

   c. $8.954 \div 1.1 =$  
   d. $17.25 \div 0.25 =$  

   e. $93.72 \div 22 =$
2. A row of tiles is 1200 centimetres long. If each tile is 2.5 centimetres long, how many tiles are needed to complete the row?

3. West Edmonton Mall requires 3 037.5 kilowatts of electricity every day. If one wind turbine can supply 22.5 kilowatts of electricity per day, how many wind turbines are required to produce enough electricity for the large mall?

4. A cross-country relay race is 172.8 kilometres long. Each runner on a team must run 10.8 kilometres. How many runners are needed for each team?
Homework Assignment

1. Calculate the answers to the following questions. Each statement needs a correct number in the blank to make it a true statement.

Example: \([(6 + 1) \times 3] – \text{__________} = 6\)
Calculate the \((6 + 1)\) first: the answer is 7
Calculate the \([(6 + 1) \times 3]\) second: the answer is \(7 \times 3 = 21\)
Then, figure out the answer: \(21 – \text{__________} = 6\)
The answer is 15 because \(21 – 15 = 6\)

a. \([(4.2 + 7.6) \times 2] – \text{__________} = 17.4\)

b. \([(9.9 \div 3) + 2.7] \times \text{__________} = 3.0\)

c. \((25.16 − 4.28 − 16.3) + \text{__________} = 9.83\)

d. \((70.14 + 8.1 + 121.12) \div \text{__________} = 62.3\)
Self-Evaluation

Ask yourself some important questions. Write your answers in sentences for your teacher.

1. In this lesson, what part of your work was excellent?

   ____________________________________________

   ____________________________________________

   ____________________________________________

2. In this lesson, what part of your work needs improvement?

   ____________________________________________

   ____________________________________________

   ____________________________________________

3. If you want help for some of the work in this lesson, ask your teacher in this space.

   ____________________________________________

   ____________________________________________

   ____________________________________________