Mathematics Grade 8 TEACHER KEY
W1 - Lesson 1: Perfect Squares and Square Roots
Important Concepts of Grade 8 Mathematics

W1 - Lesson 1 .................................................. Perfect Squares and Square Roots
W1 - Lesson 2 .................................................. Working with Ratios and Rates
W1 - Lesson 3 .................................................. Multiplying and Dividing Fractions
W1 - Lesson 4 .................................................. Multiplying and Dividing Integers
W1 - Lesson 5 .................................................. Working with Percents
W1 - Review
W1 - Quiz

W2 - Lesson 1 ..... Modelling and Solving Linear Equations Using Algebra Tiles
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W3 - Lesson 4 .................................................. Drawing 3-D Objects
W3 - Lesson 5 .................................................. Congruence of Polygons
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W3 - Quiz

Materials Required
Protractor
Ruler
Calculator

No Textbook Required
This is a stand-alone course.

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Preview/Review Concepts for Grade Eight Mathematics

Teacher Key

W1 – Lesson 1:
Perfect Squares and Square Roots
OBJECTIVES

By the end of this lesson, you will be able to:

- Determine the factors of a perfect square
- Identify a perfect square
- Determine the square of a given number
- Estimate approximate square roots with and without technology

GLOSSARY

**Factors** – the numbers that are multiplied to give a product. A factor of a given number will divide into the given number with no remainder left over. For example, the 4 and 5 are factors of 20.

**Non-perfect square** – a number that has a non-terminating and non-repeating decimal number as its square root

**Perfect square** – a number that has a whole number as its square root

**Square root** – a number that when multiplied by itself results in a specific number
W1 – Lesson 1: Perfect Squares and Square Roots

Materials required:

- Paper, Pencil, Calculator, and Grid paper

Part 1: Perfect Squares

A perfect square is a number that is the product of one number being multiplied by itself. They are called perfect squares because they form a square when they are laid out using algebra tiles.

\[
\begin{align*}
1 \times 1 &= 1 \\
2 \times 2 &= 4 \\
3 \times 3 &= 9 \\
4 \times 4 &= 16
\end{align*}
\]

The length and width of the squares are identical.

Perfect squares have an odd number of factors.

\[
\begin{align*}
12 &= 1 \times 12 \\
&= 2 \times 6 \quad \text{not a perfect square} \\
&= 3 \times 4 \quad \text{even number of factors}
\end{align*}
\]

\[
\begin{align*}
36 &= 1 \times 36 \\
&= 2 \times 18 \\
&= 3 \times 12 \\
&= 4 \times 9 \\
&= 6 \times 6
\end{align*}
\]

In this example, the number 6 can only be counted once, therefore 36 will have an odd number of factors.
Practice Questions

1. Represent the following perfect squares using the grid provided.

   a. 64

   ![Grid for 64]

   b. 121

   ![Grid for 121]
2. Identify the perfect squares in the following list of numbers. Explain why they are or are not perfect squares.

<p>| | | | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>169</td>
<td>45</td>
<td>72</td>
<td>100</td>
<td>49</td>
<td>56</td>
</tr>
</tbody>
</table>

169 - this is a perfect square because it has an odd number of factors
45 - this is a non-perfect square because it has an even number of factors
72 - this is a non-perfect square because it has an even number of factors
100 - this is a perfect square because it has an odd number of factors
49 - this is a perfect square because it has an odd number of factors
56 - this is a non-perfect square because it has an even number of factors
Part 2: Square Roots

In the previous examples involving counting factors of numbers, you looked at the factors of perfect squares. You understand that perfect squares have an odd number of factors. Since 6 is multiplied by itself to get 36, 6 is the square root of 36.

A square root is the number being multiplied by itself that results in a specific number.

The symbol that represents a square root is $\sqrt{}$.

You can calculate the square root of a number mentally or using a calculator. When asked to find the square root of a given number, ask yourself “What number do I multiply by itself to result in a product of the given number?”

Or press the $\sqrt{}$ on your calculator and then type in the number.

Example 1

What is the square root of 25? This is expressed mathematically as $\sqrt{25}$.

Mentally:

“What number is multiplied by itself to result in a product of 25?”

The answer is 5.

Calculator:

Type in $\sqrt{25}$ or $25\sqrt{}$ depending on your calculator.

The screen will show an answer of 5.
Example 1

1. \(\sqrt{400}\)

\[\sqrt{400} = 20\]

2. \(\sqrt{289}\)

\[\sqrt{289} = 17\]

3. \(\sqrt{225}\)

\[\sqrt{225} = 15\]

Determine the square of the following numbers.

4. 11

\[11^2 = 121\]

5. 16

\[16^2 = 256\]

6. 9

\[9^2 = 81\]
Part 3: Approximate Square Roots

Only perfect squares will have square roots that are whole numbers. Non-perfect squares will have square roots that are decimal numbers. The number 30 is a non-perfect square because when you type in \( \sqrt{30} \) into your calculator, the following number will appear, 5.47725575... This decimal does not terminate or repeat, it will go on forever. In these cases, you must approximate the answer. A reasonable answer for the square root of 30 is 5.47.

\[ \sqrt{30} \approx 5.47 \]

You can also approximate square roots without using a calculator.

For example, the \( \sqrt{15} \) can be determined using your knowledge of other commonly used perfect squares. The number 15 is in between the perfect squares 9 and 16. The square root of 9 is 3. The square root of 16 is 4.

This tells you that the square root of 15 is somewhere between 3 and 4. Since 15 is closer to 16 than it is to 9, the square root of 15 will be closer to 4.

A good estimate is 3.9. Thus, \( \sqrt{15} \approx 3.9 \).
Practice Questions

Approximate the square roots of the following numbers using a calculator. Round your answer to the nearest hundredth.

1. \(\sqrt{55} \approx \)  
   \[\sqrt{55} \approx 7.42\]

2. \(\sqrt{92} \approx \)  
   \[\sqrt{92} \approx 9.59\]

3. \(\sqrt{76} \approx \)  
   \[\sqrt{76} \approx 8.72\]

Determine the two numbers in which the square root of the following numbers falls in between.

4. \(\sqrt{61}\) is in between \(7\) & \(8\)

5. \(\sqrt{35}\) is in between \(5\) & \(6\)

6. \(\sqrt{84}\) is in between \(9\) & \(10\)
Lesson 1: Assignment

1. Express the following numbers as perfect squares on the grid provided:
   a. 49
      ![Grid for 49]
   b. 144
      ![Grid for 144]
2. Determine which of the following numbers are perfect squares using their factors as a guide.

196 27 100 63 50

196- this is a perfect square because it has an odd number of factors
27- this is a non-perfect square because it has an even number of factors
100- this is a perfect square because it has an odd number of factors
63- this is a non-perfect square because it has an even number of factors
50- this is a non-perfect square because it has an even number of factors

3. Determine the square root of the following numbers

a. \( \sqrt{529} \)

\( \sqrt{529} = 23 \)

b. \( \sqrt{961} \)

\( \sqrt{961} = 31 \)

c. \( \sqrt{784} \)

\( \sqrt{784} = 28 \)

d. \( \sqrt{121} \)

\( \sqrt{121} = 11 \)
4. Determine the square of the following numbers.
   a. 6 \[ 6^2 = 36 \]
   b. 25 \[ 25^2 = 625 \]
   c. 100 \[ 100^2 = 10000 \]
   d. 14 \[ 14^2 = 196 \]

5. Use your calculator to find the square roots of the following numbers. Round the answer to the nearest tenth.
   a. \[ \sqrt{117} \approx 10.8 \]
   b. \[ \sqrt{285} \approx 16.9 \]
   c. \[ \sqrt{3030} \approx 55.0 \]
   d. \[ \sqrt{99} \approx 9.9 \]